

Package: bitriad (via r-universe)

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Type Package

Title Triadic Analysis of Affiliation Networks

Version 0.4

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Description Two principal tools are provided for the triadic analysis of affiliation networks: triad census and triadic closure. These include several variations on both classical tools tailored to affiliation network structure; see Opsahl (2013) <[doi:10.1016/j.socnet.2011.07.001](https://doi.org/10.1016/j.socnet.2011.07.001)>, Liebig and Rao (2014) <[doi:10.1109/SITIS.2014.15](https://doi.org/10.1109/SITIS.2014.15)>, and Brunson (2015) <[doi:10.1017/nws.2015.38](https://doi.org/10.1017/nws.2015.38)>. Additional functions support manipulation of affiliation networks. Built on 'igraph' with new C++ calculations exposed via 'Rcpp'.

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affiliation_network *Affiliation network structure*

Description

Test igraph objects for affiliation network structure or impose such structure if possible.

Usage

`is_an(graph)`

`is.an(graph)`

`as_an(graph, map_type = FALSE)`

`as.an(graph, map_type = FALSE)`

Arguments

graph	An igraph object.
map_type	Logical; whether to add a type attribute for bipartite structure if graph admits one.

Details

An affiliation network is a bipartite graph whose nodes are classified as actors and events in such a way that all links are between actors and events. The function `is_bipartite()` tests an igraph object for a type attribute, which is intended to bipartition of the nodes. It does not test whether the links respect this partition. The function `is_an` tests this, as well as the condition that actor nodes precede event nodes in their node IDs, which simplifies some other functions. The function `as_an` coerces an igraph object to an affiliation network by verifying that the object is bipartite and minimally permuting the node IDs. If graph has no type attribute and `map_type` is FALSE, then `as_an` throws an error; if `map_type` is TRUE, then `as_an` calls `bipartite_mapping()` to add a logical type attribute that takes the value FALSE at the first node (by node ID) in each connected component and TRUE or FALSE at the remaining nodes. (If this cannot be done, an error is thrown.)

Value

For `is_an()`, a logical value; for `as_an()`, the input graph with a "type" attribute.

See Also

Original **igraph** functions: `is_igraph()`

Other network testing and coercion: `dynamic_an`

Examples

```
graph <- make_graph(c( 1,2, 1,4, 1,6, 3,6, 5,6, 7,8, 9,8 ))
is_an(graph)
# as_an(graph) # throws an error
an_graph <- as_an(graph, map_type = TRUE)
is_an(an_graph)
```

bitriad

bitriad: *Triadic analysis of affiliation networks*

Description

Calculate triad censuses and triad closure statistics designed for affiliation networks.

Details

The package contains two principal tools for the triadic analysis of affiliation networks: triad censuses and measures of triad closure. Assorted additional functions, including a measure of dynamic triad closure, are also included.

Triad censuses

Three triad censuses are implemented for affiliation networks:

- The *full triad census* (Brunson, 2015) records the number of triads of each isomorphism class. The classes are indexed by a partition, $\lambda = (\lambda_1 \leq \lambda_2 \leq \lambda_3)$, indicating the number of events attended by both actors in each pair but not the third, and a positive integer, w , indicating the number of events attended by all three actors. The isomorphism classes are organized into a matrix with rows indexed by λ and columns indexed by w , with the partitions λ ordered according to the *revolving door ordering* (Kreher & Stinson, 1999). The main function `triad_census_an` (called from `triad_census` when the graph argument is an `affiliation_network`) defaults to this census.
- For the analysis of sparse affiliation networks, the full triad census may be less useful than information on whether the extent of connectivity through co-attended events differs between each pair of actors. In order to summarize this information, a coarser triad census can be conducted on classes of triads based on the following congruence relation: Using the indices $\lambda = (x \geq y \geq z)$ and w above, note that the numbers of shared events for each pair and for the triad are $x+w \geq y+w \geq z+w \geq w \geq 0$. Consider two triads congruent if the same subset of these weak inequalities are strictly satisfied. The resulting *difference triad census*, previously called the *uniformity triad census*, implemented as `triad_census_difference`, is organized into a 8×2 matrix with the strictness of the first three inequalities determining the row and that of the last inequality determining the column.
- A still coarser congruence relation can be used to tally how many are connected by at least one event in each distinct way. This relation considers two triads congruent if each corresponding pair of actors both attended or did not attend at least one event not attended by the third, and if the corresponding triads both attended or did not attend at least one event together. The *binary triad census* (Brunson, 2015; therein called the *structural triad census*), implemented as `triad_census_binary`, records the number of triads in each congruence class.
- The *simple triad census* is the 4-entry triad census on a traditional (non-affiliation) network indicating the number of triads of each isomorphism class, namely whether the triad contains zero, one, two, or three links. The function `simple_triad_census` computes the classical (undirected) triad census for an undirected traditional network, or for the actor projection of an affiliation network (if provided), using `triad_census`; if the result doesn't make sense (i.e., the sum of the entries is not the number of triples of nodes), then it instead uses its own, much slower method.

Each of these censuses can be projected from the previous using the function `project_census`. A fourth census, called the *uniformity triad census* and implemented as `unif_triad_census`, is deprecated. Three-actor triad affiliation networks can be constructed and plotted using the `triad` functions.

The default method for the two affiliation network-specific triad censuses is adapted from the algorithm of Batagelj and Mrvar (2001) for calculating the classical triad census for a directed graph.

Measures of triad closure

Each measure of triad closure is defined as the proportion of wedges that are closed, where a *wedge* is the image of a specified two-event triad W under a specified subcategory of graph maps C subject to a specified congruence relation \sim , and where a wedge is *closed* if it is the image of such a map that factors through a canonical inclusion of W to a specified self-dual three-event triad X .

The alcove, wedge, maps, and congruence can be specified by numerical codes as follows (no plans exist to implement more measures than these):

- alcove:
 - 0: $T_{(1,1,1),0}$
 - 1: $T_{(1,1,0),1}$ (**not yet implemented**)
 - 2: $T_{(1,0,0),2}$ (**not yet implemented**)
 - 3: $T_{(0,0,0),3}$ (**not yet implemented**)
- wedge:
 - 0: $T_{(1,1,0),0}$
 - 1: $T_{(1,0,0),1}$ (**not yet implemented**)
 - 2: $T_{(0,0,0),2}$ (**not yet implemented**)
- maps:
 - 0: all graph maps (injective on actors)
 - 1: injective graph maps
 - 2: induced injective graph maps
- congruence:
 - 0: same actor and event images (equivalence)
 - 1: same actor images, structurally equivalent event images
 - 2: same actor images

Some specifications correspond to statistics of especial interest:

- 0, 0, 0, 2: the classical clustering coefficient (Watts & Strogatz, 1998), evaluated on the unipartite actor projection
- 0, 0, 1, 0: the two-mode clustering coefficient (Opsahl, 2013)
- 0, 0, 2, 0: the unconnected clustering coefficient (Liebig & Rao, 2014)
- 3, 2, 2, 0: the completely connected clustering coefficient (Liebig & Rao, 2014) (**not yet implemented**)
- 0, 0, 2, 1: the exclusive clustering coefficient (Brunson, 2015)
- 0, 0, 2, 2: the exclusive clustering coefficient

See Brunson (2015) for a general definition and the aforementioned references for discussions of each statistic.

Author(s)

Jason Cory Brunson

References

- Kreher, D.L., & Stinson, D.R. (1999). Combinatorial algorithms: generation, enumeration, and search. *SIGACT News*, 30(1), 33–35.
- Batagelj, V., & Mrvar, A. (2001). A subquadratic triad census algorithm for large sparse networks with small maximum degree. *Social Networks*, 23(3), 237–243.
- Brunson, J.C. (2015). Triadic analysis of affiliation networks. *Network Science*, 3(4), 480–508.

Watts, D.J., & Strogatz, S.H. (1998). Collective dynamics of "small-world" networks. *Nature*, 393(6684), 440–442.

Opsahl, T. (2013). Triadic closure in two-mode networks: Redefining the global and local clustering coefficients. *Social Networks*, 35(2), 159–167. Special Issue on Advances in Two-mode Social Networks.

Liebig, J., & Rao, A. (2014). Identifying influential nodes in bipartite networks using the clustering coefficient. Pages 323–330 of: *Proceedings of the tenth international conference on signal-image technology and internet-based systems*.

Brunson, J.C. (2015). Triadic analysis of affiliation networks. *Network Science*, 3(4), 480–508.

See Also

Useful links:

- <http://corybrunson.github.io/bitriad/>

chicago1960s

Corporate interlocks among directors in Chicago.

Description

An affiliation network of 20 directors of 24 corporations and social clubs.

Format

An affiliation network; see [is_an](#).

Source

Barnes, R. & Burkett, T. (2010). Structural Redundancy and Multiplicity in Corporate Networks. *Connections*, 30(2), p. 4–20. <https://www.insna.org/connections-archives-2000-2015>

dualize

Take the dual of an affiliation network

Description

This function obtains the dual of an affiliation network, in which the actors and events have swapped roles. To do this, it negates the logical values of the node type attribute and reorders the node ids accordingly.

Usage

```
dualize(graph)
```

```
dual_an(graph)
```

```
dual.an(graph)
```

Arguments

graph An affiliation network.

Value

The input graph with the "type" attribute logically negated.

See Also

Other modal queries and manipulations: [mode_addition](#), [mode_counts](#), [modes](#), [schedule\(\)](#)

Examples

```
data(women_clique)
( tab <- table(V(women_clique)$type) )
( proj <- actor_projection(dualize(women_clique)) )
vcount(proj) == tab[2]
```

dynamic_an

Dynamic affiliation network structure

Description

An affiliation network is *dynamic*, for present purposes, if its event nodes have time stamps, recorded as a numeric vertex attribute "time" in non-decreasing order.

Usage

```
is_dynamic_an(graph)
```

```
is.dyn(graph)
```

```
as_dynamic_an(graph, use_attr = NULL)
```

Arguments

graph An affiliation network.

use_attr Character; the vertex attribute to coerce to numeric if necessary and use as the "time" attribute. If NULL, the default, time takes the values `seq(event_count(graph))`, reflecting the order of the event node IDs.

Value

The input graph with a new "time" vertex attribute and its event nodes permuted to respect this attribute.

See Also

Other network testing and coercion: [affiliation_network](#)

Examples

```
data(women_group)
is_dynamic_an(women_group)
data(women_clique)
is_dynamic_an(women_clique)
as_dynamic_an(women_clique)
data(nmt_meetings)
nmt_meetings <- set_event_attr(
  nmt_meetings, "meet",
  value = gsub("meet", "", V2(nmt_meetings)$name)
)
as_dynamic_an(nmt_meetings, use_attr = "meet")
```

dynamic_triad_closure *Triadic closure for dynamic affiliation networks*

Description

Given an affiliation network with time-stamped events, compute the proportion of centered triples at which an open wedge exists at some time that is closed at a later time.

Usage

```
dynamic_triad_closure(
  graph,
  actors = V(graph)[V(graph)$type == FALSE],
  type = "global",
  ...,
  measure = NULL
)

dynamic_triad_closure_an(
  graph,
  actors = V(graph)[V(graph)$type == FALSE],
  type = "global",
  ...,
  measure = NULL
)
```

```

dynamic_transitivity_an(
  graph,
  actors = V(graph)[V(graph)$type == FALSE],
  type = "global",
  ...,
  measure = NULL
)

dyn.transitivity.an(
  graph,
  actors = V(graph)[V(graph)$type == FALSE],
  type = "global",
  ...,
  measure = NULL
)

dynamic_triad_closure_projection(graph, memory = Inf, type = "global")

```

Arguments

graph	An affiliation network with time-stamped events.
actors	A vector of actor nodes in graph.
type	The type of statistic, matched to "global", "local", or "raw".
...	Additional parameters passed to specific functions.
measure	Character; the measure of triad closure, used as the suffix * to triad_closure_*. Matched to "classical" (also "watts_strogatz"), "twomode" (also "opsahl"), "unconnected" (also "liebig_rao_0"), "completely_connected" (also "liebig_rao_3"), "exclusive", or "projection".
memory	Numeric; minimum delay of wedge formation since would-have-been closing events.

Value

A numeric vector of the same length as actors.

See Also

Other triad closure functions: [project_transitivity\(\)](#), [transitivity_an\(\)](#), [triad_closure\(\)](#), [triad_closure_from_census\(\)](#)

Examples

```

data(women_group)
dynamic_triad_closure(women_group)
cbind(
  transitivity(actor_projection(women_group), type = "local"),
  triad_closure_opsahl(women_group, type = "local"),

```

```

    triad_closure_exclusive(women_group, type = "local"),
    dynamic_triad_closure_projection(women_group, type = "local"),
    dynamic_triad_closure(women_group, type = "local")
)

```

dynamic_wedges	<i>Wedge censuses and closure indicators for dynamic affiliation networks</i>
----------------	---

Description

Given a dynamic affiliation network and an actor node ID, identify all wedges for a specified measure centered at the node and indicate whether each is closed.

Usage

```

dynamic_wedges(
  graph,
  actor,
  alcove = 0,
  wedge = 0,
  maps = 0,
  congruence = 0,
  memory = Inf,
  wedge.gap = Inf,
  close.after = 0,
  close.before = Inf
)

```

Arguments

graph	A dynamic affiliation network.
actor	An actor node in graph.
alcove, wedge, maps, congruence	Choice of alcove, wedge, maps, and congruence (see Details).
memory	Numeric; minimum delay of wedge formation since would-have-been closing events.
wedge.gap	Numeric; maximum delay between the two events of a wedge.
close.after, close.before	Numeric; minimum and maximum delays after both events form a wedge for a third event to close it.

Details

The `dynamic_wedges_*` functions implement wedge censuses underlying the several measures of triad closure described below. Each function returns a transversal of wedges from the congruence classes of wedges centered at the index actor and indicators of whether each class is closed. The shell function `dynamic_wedges` determines a unique measure from several coded arguments (see below) and passes the input affiliation network to that measure.

Value

A two-element list consisting of (1) a 3- or 5-row integer matrix of (representatives of) all (congruence classes of) wedges in graph centered at actor, and (2) a logical vector indicating whether each wedge is closed.

Measures of triad closure

Each measure of triad closure is defined as the proportion of wedges that are closed, where a *wedge* is the image of a specified two-event triad W under a specified subcategory of graph maps C subject to a specified congruence relation, and where a wedge is *closed* if it is the image of such a map that factors through a canonical inclusion of W to a specified self-dual three-event triad X .

The alcove, wedge, maps, and congruence can be specified by numerical codes as follows (no plans exist to implement more measures than these):

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 - 1: $T_{(1,1,0),1}$ (**not yet implemented**)
 - 2: $T_{(1,0,0),2}$ (**not yet implemented**)
 - 3: $T_{(0,0,0),3}$ (**not yet implemented**)
- wedge:
 - 0: $T_{(1,1,0),0}$
 - 1: $T_{(1,0,0),1}$ (**not yet implemented**)
 - 2: $T_{(0,0,0),2}$ (**not yet implemented**)
- maps:
 - 0: all graph maps (injective on actors)
 - 1: injective graph maps
 - 2: induced injective graph maps
- congruence:
 - 0: same actor and event images (equivalence)
 - 1: same actor images, structurally equivalent event images
 - 2: same actor images

Some specifications correspond to statistics of especial interest:

- $0, 0, 0, 2$: the classical clustering coefficient (Watts & Strogatz, 1998), evaluated on the unipartite actor projection
- $0, 0, 1, 0$: the two-mode clustering coefficient (Opsahl, 2013)
- $0, 0, 2, 0$: the unconnected clustering coefficient (Liebig & Rao, 2014)
- $3, 2, 2, 0$: the completely connected clustering coefficient (Liebig & Rao, 2014) (**not yet implemented**)
- $0, 0, 2, 1$: the exclusive clustering coefficient (Brunson, 2015)
- $0, 0, 2, 2$: the exclusive clustering coefficient

See Brunson (2015) for a general definition and the aforementioned references for discussions of each statistic.

References

Watts, D.J., & Strogatz, S.H. (1998). Collective dynamics of "small-world" networks. *Nature*, 393(6684), 440–442.

Opsahl, T. (2013). Triadic closure in two-mode networks: Redefining the global and local clustering coefficients. *Social Networks*, 35(2), 159–167. Special Issue on Advances in Two-mode Social Networks.

Liebig, J., & Rao, A. (2014). Identifying influential nodes in bipartite networks using the clustering coefficient. Pages 323–330 of: *Proceedings of the tenth international conference on signal-image technology and internet-based systems*.

Brunson, J.C. (2015). Triadic analysis of affiliation networks. *Network Science*, 3(4), 480–508.

See Also

Other wedge functions: [indequ_wedges\(\)](#)

index_subset

Combinatorial bijections for affiliation network triad indexing

Description

These functions biject among partitions of at most 3 parts, 3-subsets of natural numbers, and indices for the lexicographic total orders on them.

Usage

`index_subset(i)`

`subset_index(vec)`

`subset_partition(vec)`

`partition_subset(lambda)`

`index_partition(i)`

`partition_index(lambda)`

`indexSubset(i)`

`indexPartition(i)`

`subsetIndex(vec)`

`subsetPartition(vec)`

`partitionIndex(lambda)`

```
partitionSubset(lambda)
```

Arguments

`i` Integer; an index in the total order, starting at 0.
`vec` Integer vector; a set of 3 distinct non-negative integers, in decreasing order.
`lambda` Integer vector; a partition of at most 3 parts, with parts in non-increasing order.

Value

Numeric vectors.

Examples

```
index_subset(2)
index_partition(2)
subset_index(c(3, 2, 0))
subset_partition(c(3, 2, 0))
partition_index(c(1, 1, 0))
partition_subset(c(1, 1, 0))
```

minneapolis1970s

Interlocks among corporate philanthropists in Minneapolis-St. Paul.

Description

These data record the memberships of 26 directors on the boards of 15 companies. They are a subset of a larger dataset that is not publicly available.

Format

An affiliation network; see [is_an](#).

Source

Wasserman, S. & Faust, K. (1994). *Social Network Analysis: Methods and Applications*. Cambridge University Press. <http://books.google.com/books?id=CAm2DpIqRUIC>

mode_addition	<i>Add actor and event nodes</i>
---------------	----------------------------------

Description

These functions add actor and event nodes (as desired) to a graph while maintaining its (temporal) affiliation network structure.

Usage

```
add_modes(graph, mode = 1, nv, ..., attr = list(), affiliations = NULL)
```

```
add_actors(graph, nv, ..., attr = list(), events = NULL)
```

```
add_events(graph, nv, ..., attr = list(), actors = NULL)
```

Arguments

graph	An affiliation network.
mode	Numeric or character; whether to project onto actors (1 or "actors") or onto events (2 or "events").
nv, ..., attr	Arguments passed to add_vertices() . Events added to a dynamic affiliation network should be given time attributes.
affiliations	A vector, or list of length nv of vectors, of nodes in graph of mode <i>not</i> mode, to be linked to the new node(s).
events	A vector, or list of length nv of vectors, of event nodes in graph, to be linked to the new actor(s).
actors	A vector, or list of length nv of vectors, of actor nodes in graph, to be linked to the new event(s).

Value

The input graph with additional actor or event nodes added.

See Also

Original **igraph** functions: [add_vertices\(\)](#), [add_edges\(\)](#)

Other modal queries and manipulations: [dualize\(\)](#), [mode_counts](#), [modes](#), [schedule\(\)](#)

Examples

```
data(women_clique)
plot(prettify_an(add_actors(women_clique, nv = 1, events = c(7, 9))))
data(women_group)
plot(prettify_an(women_group))
actor_names <- c("Frances", "Dorothy")
```

```

cbind(
  dynamic_triad_closure(women_group, type = "local"),
  dynamic_triad_closure(
    add_events(women_group, nv = 1, actors = actor_names, time = 0),
    type = "local"
  ),
  dynamic_triad_closure(
    add_events(women_group, nv = 1, actors = actor_names, time = 367),
    type = "local"
  )
)

```

mode_counts

Count the actors and events in an affiliation network

Description

These functions return the number of actors (nodes with type attribute FALSE) or events (TRUE) in an affiliation network.

Usage

```
actor_count(graph)
```

```
event_count(graph)
```

```
actor.count(graph)
```

```
event.count(graph)
```

Arguments

graph An affiliation network.

Value

An integer.

See Also

Original **igraph** functions: [vcount\(\)](#), [ecount\(\)](#)

Other modal queries and manipulations: [dualize\(\)](#), [mode_addition](#), [modes](#), [schedule\(\)](#)

Examples

```

data(chicago1960s)
actor_count(chicago1960s)
event_count(chicago1960s)

```

mode_projection	<i>Project an affiliation network onto its actors</i>
-----------------	---

Description

These functions use `bipartite_projection()` to compute the projections of an affiliation network onto the actor or event nodes.

Usage

```
mode_projection(graph, mode = 1, name = "name")
actor_projection(graph, ...)
event_projection(graph, ...)
actor.projection(graph, ...)
event.projection(graph, ...)
```

Arguments

graph	An affiliation network.
mode	Numeric or character; whether to project onto actors (1 or "actors") or onto events (2 or "events").
name	Character; the attribute of the actor or event nodes in graph to use as names for the nodes in the projection. If NA, node IDs are converted to characters and used. If NULL, no names are assigned.
...	Arguments passed to mode_projection.

Value

An igraph object with nodes corresponding to one "type" of the input graph.

See Also

Original **igraph** functions: `bipartite_projection()`

Examples

```
data(chicago1960s)
( tab <- table(V(chicago1960s)$type) )
( proj <- actor_projection(chicago1960s) )
vcount(proj) == tab[1]
( proj <- event_projection(chicago1960s) )
vcount(proj) == tab[2]
```

Description

These functions return actor and event node lists.

Usage

```
V1(graph)
```

```
V2(graph)
```

```
actor_attr(graph, name, index = V1(graph))
```

```
event_attr(graph, name, index = V2(graph))
```

```
set_actor_attr(graph, name, index = V1(graph), value)
```

```
set_event_attr(graph, name, index = V2(graph), value)
```

```
V1(x) <- value
```

```
V2(x) <- value
```

Arguments

graph	An affiliation network.
name	The name of the attribute to set.
index	An optional node sequence to set the attributes of a subset of actor or event nodes.
value	The new value of the attribute for all (or index) actor or event nodes.
x	An affiliation network.

Value

The value of the actor or event attribute, or the input graph with the attribute set.

See Also

Original **igraph** functions: [V\(\)](#), [vertex_attr\(\)](#), [set_vertex_attr\(\)](#)

Other modal queries and manipulations: [dualize\(\)](#), [mode_addition](#), [mode_counts](#), [schedule\(\)](#)

Examples

```
data(women_clique)
print(V1(women_clique))
print(V2(women_clique))
V1(women_clique)$label <- LETTERS[1:5]
V2(women_clique)$label <- 1:5
plot(prettify_an(women_clique))
```

nmt_meetings

Noordin Top meeting attendance network.

Description

These data record the attendance of 26 individuals at 20 meetings associated with Noordin Mohammad Top.

Format

An affiliation network; see [is_an](#).

Source

Noordin Top Terrorist Network Data. (2011). The Association of Religious Data Archives. <https://web.archive.org/web/20140625114607/http://www.thearda.com/Archive/Files/Descriptions/TERRNET.asp>

nmt_organizations

Noordin Top organization membership network.

Description

These data record the attendance of 67 members of 32 organizations associated with Noordin Mohammad Top.

Format

An affiliation network; see [is_an](#).

Source

Noordin Top Terrorist Network Data. (2011). The Association of Religious Data Archives. <https://web.archive.org/web/20140625114607/http://www.thearda.com/Archive/Files/Descriptions/TERRNET.asp>

prettify

Convenient plotting aesthetics for affiliation networks

Description

Given an affiliation network, assign the node and link aesthetics to values that produce a neater visualization through [plot.igraph](#) than the **igraph** defaults.

Usage

```
prettify_an(graph)
```

```
prettify.an(graph)
```

Arguments

graph An affiliation network.

Value

The input graph with aesthetic node and link attributes (re)set.

Examples

```
library(igraph)
data(women_clique)
data(whigs)
for (g in list(women_clique, whigs)) {
  plot(prettify_an(g))
}
```

project_census

Project a higher-resolution triad census to a lower-resolution one

Description

Given a triad census of any scheme, construct a triad census of a coarser (strictly less informative) scheme.

Usage

```

project_census(census, scheme = NULL, add.names = TRUE)

project.census(census, scheme = NULL, add.names = TRUE)

difference_from_full_census(census)

ftc2utc(census)

binary_from_full_census(census)

ftc2stc(census)

simple_from_full_census(census)

ftc2tc(census)

binary_from_difference_census(census)

utc2stc(census)

simple_from_difference_census(census)

utc2tc(census)

simple_from_binary_census(census)

stc2tc(census)

```

Arguments

census	Numeric matrix or vector; an affiliation network triad census. It is treated as binary or simple if its dimensions are 4-by-2 or 4-by-1, respectively, unless otherwise specified by scheme; otherwise it is treated as full.
scheme	Character; the type of triad census provided, matched to "full", "difference" (also "uniformity"), "binary" (also "structural"), or "simple".
add.names	Logical; whether to label the rows and columns of the output matrix.

Details

This function inputs an affiliation network triad census of any scheme and returns a list of triad censuses projected from it (not including itself). The schemes are, in order of resolution, *full* (also called the *affiliation network triad census* without qualification), *difference*, *binary*, and *simple*. A final element of the output list is the total number of triads in the affiliation network. Each summary can be recovered from those before it, specifically by aggregating certain matrix entries to form a smaller matrix. The helper functions `*_from*_census()` project a census of each scheme to one of each coarser scheme.

Value

A list of `triad_census()` outputs.

Triad censuses

Three triad censuses are implemented for affiliation networks:

- The *full triad census* (Brunson, 2015) records the number of triads of each isomorphism class. The classes are indexed by a partition, $\lambda = (\lambda_1 \leq \lambda_2 \leq \lambda_3)$, indicating the number of events attended by both actors in each pair but not the third, and a positive integer, w , indicating the number of events attended by all three actors. The isomorphism classes are organized into a matrix with rows indexed by λ and columns indexed by w , with the partitions λ ordered according to the *revolving door ordering* (Kreher & Stinson, 1999). The main function `triad_census_an` (called from `triad_census` when the graph argument is an `affiliation_network`) defaults to this census.
- For the analysis of sparse affiliation networks, the full triad census may be less useful than information on whether the extent of connectivity through co-attended events differs between each pair of actors. In order to summarize this information, a coarser triad census can be conducted on classes of triads based on the following congruence relation: Using the indices $\lambda = (x \geq y \geq z)$ and w above, note that the numbers of shared events for each pair and for the triad are $x+w \geq y+w \geq z+w \geq w \geq 0$. Consider two triads congruent if the same subset of these weak inequalities are strictly satisfied. The resulting *difference triad census*, previously called the *uniformity triad census*, implemented as `triad_census_difference`, is organized into a 8×2 matrix with the strictness of the first three inequalities determining the row and that of the last inequality determining the column.
- A still coarser congruence relation can be used to tally how many are connected by at least one event in each distinct way. This relation considers two triads congruent if each corresponding pair of actors both attended or did not attend at least one event not attended by the third, and if the corresponding triads both attended or did not attend at least one event together. The *binary triad census* (Brunson, 2015; therein called the *structural triad census*), implemented as `triad_census_binary`, records the number of triads in each congruence class.
- The *simple triad census* is the 4-entry triad census on a traditional (non-affiliation) network indicating the number of triads of each isomorphism class, namely whether the triad contains zero, one, two, or three links. The function `simple_triad_census` computes the classical (undirected) triad census for an undirected traditional network, or for the actor projection of an affiliation network (if provided), using `triad_census`; if the result doesn't make sense (i.e., the sum of the entries is not the number of triples of nodes), then it instead uses its own, much slower method.

Each of these censuses can be projected from the previous using the function `project_census`. A fourth census, called the *uniformity triad census* and implemented as `unif_triad_census`, is deprecated. Three-actor triad affiliation networks can be constructed and plotted using the `triad` functions.

The default method for the two affiliation network-specific triad censuses is adapted from the algorithm of Batagelj and Mrvar (2001) for calculating the classical triad census for a directed graph.

References

Kreher, D.L., & Stinson, D.R. (1999). Combinatorial algorithms: generation, enumeration, and search. *SIGACT News*, 30(1), 33–35.

Batagelj, V., & Mrvar, A. (2001). A subquadratic triad census algorithm for large sparse networks with small maximum degree. *Social Networks*, 23(3), 237–243.

Brunson, J.C. (2015). Triadic analysis of affiliation networks. *Network Science*, 3(4), 480–508.

See Also

Other triad census functions: [triad_census\(\)](#), [triad_closure_from_census\(\)](#), [triad_tallies](#)

Examples

```
data(women_group)
group_full_census <- triad_census(women_group, scheme = "full")
project_census(group_full_census, scheme = "full")
group_binary_census <- triad_census(women_group, scheme = "binary")
project_census(group_binary_census, scheme = "binary")
```

project_transitivity *Affiliation network clustering coefficients*

Description

Each clustering coefficient can be defined as the proportion of "wedges" that are "closed", for suitable definitions of both terms. The main function, [transitivity_an\(\)](#), calls one of the wedge functions and computes the global or local clustering coefficient of the given affiliation network, and if the local, then at the given nodes. ([project_transitivity](#) cheats by using [transitivity\(\)](#) but produces output consistent with the other variants of [transitivity_an\(\)](#).)

Usage

```
project_transitivity(graph, type = "global", vids = which(!V(graph)$type))
```

```
project.transitivity(graph, type = "global", vids = which(!V(graph)$type))
```

Arguments

graph	An affiliation network.
type	The type of clustering coefficient (defaults to "global")
vids	A subset of actor node ids at which to evaluate the local clustering coefficient.

Value

If type is "global", the global clustering coefficient of the network (a single numeric value); if "local", the local clustering coefficients of the actors (a numeric vector); otherwise, a 2-column matrix, each row of which gives the number of wedges and the number of closed wedges centered at each actor.

See Also

Other triad closure functions: [dynamic_triad_closure\(\)](#), [transitivity_an\(\)](#), [triad_closure\(\)](#), [triad_closure_from_census\(\)](#)

 schedule

Actors and their shared events

Description

Given an affiliation network and a vector of actor node IDs, produce the induced subgraph on the actor nodes together with all event nodes incident to at least two of them. This is called the actors' *schedule*.

Usage

```
schedule(graph, actors = V(graph)[V(graph)$type == FALSE])
```

Arguments

graph	An affiliation network.
actors	A vector of actor nodes in graph.

Value

An igraph object induced from the input graph.

See Also

Other modal queries and manipulations: [dualize\(\)](#), [mode_addition](#), [mode_counts](#), [modes](#)

Examples

```
data(women_clique)
schedule(women_clique, actors = V1(women_clique)[seq(3)])
```

 scotland1920s

Networks of interlocking directorates

Description

Five affiliation networks constructed from the multiple directors lists of the top >100 Scottish companies over five two-year intervals between 1904 and 1974.

Format

An affiliation network; see [is_an](#).

Source

Scott, J., & Hughes, M. (1980). *The Anatomy of Scottish Capital*. Croom Helm. <http://books.google.com/books?id=59mvAwAAQBAJ>

 transitivity_an

Affiliation network clustering coefficients

Description

This function computes a given flavor of transitivity (triadic closure) on a given affiliation network. The calculations are performed locally. Each flavor is defined as a proportion of "wedges" that are "closed", for suitable definitions of both terms. The function `transitivity_an` is a shell that proceeds across actors and computes wedges using the provided `wedgeFun`. These functions count the "wedges", and among them the "closed" ones, centered at a given actor node in a given affiliation network. The triads method `transitivity_an_triads` first classifies every triad centered at each node. The appropriate formula then counts the wedges and closed wedges at each. The method is slower for a single flavor but can be used to produce multiple flavors with negligible additional computational cost. The wedges method `transitivity_an_wedges` relies on a separate "wedge function" for each statistic. The algorithm calls the appropriate wedge function to run over the necessary wedge centers and return a wedge count matrix, which is returned back into `transitivity_an` for outputting.

Usage

```
transitivity_an(
  graph,
  type = "global",
  wedgeFun,
  flavor,
  vids = which(!V(graph)$type),
  add.names = FALSE
)
```

```
transitivity_an_triads(graph, vids = which(!V(graph)$type), flavor)

transitivity_an_wedges(graph, vids = which(!V(graph)$type), wedgeFun)

transitivity.an(
  graph,
  type = "global",
  wedgeFun,
  flavor,
  vids = which(!V(graph)$type),
  add.names = FALSE
)

transitivity.an.triads(graph, vids = which(!V(graph)$type), flavor)

transitivity.an.wedges(graph, vids = which(!V(graph)$type), wedgeFun)

indequ_transitivity(graph, type = "global", vids = which(!V(graph)$type))
indequ.transitivity(graph, type = "global", vids = which(!V(graph)$type))
indstr_transitivity(graph, type = "global", vids = which(!V(graph)$type))
indstr.transitivity(graph, type = "global", vids = which(!V(graph)$type))
injact_transitivity(graph, type = "global", vids = which(!V(graph)$type))
injact.transitivity(graph, type = "global", vids = which(!V(graph)$type))
injequ_transitivity(graph, type = "global", vids = which(!V(graph)$type))
injequ.transitivity(graph, type = "global", vids = which(!V(graph)$type))
injstr_transitivity(graph, type = "global", vids = which(!V(graph)$type))
injstr.transitivity(graph, type = "global", vids = which(!V(graph)$type))
opsahl_transitivity(graph, type = "global", vids = which(!V(graph)$type))
opsahl.transitivity(graph, type = "global", vids = which(!V(graph)$type))
excl_transitivity(graph, type = "global", vids = which(!V(graph)$type))
excl.transitivity(graph, type = "global", vids = which(!V(graph)$type))
```

Arguments

graph An affiliation network; see `is_an`.

type	Character; the type of clustering coefficient (defaults to "global").
wedgeFun	The wedge function; overrides flavor.
flavor	The flavor of transitivity to be used; overridden by wedgeFun.
vids	A subset of actor node ids at which to evaluate the local clustering coefficient.
add.names	Logical; whether to label the matrix rows and columns.
triads	A matrix of centered triads.

Value

If type is "global", the global clustering coefficient of the network (a single numeric value); if "local", the local clustering coefficients of the actors (a numeric vector); otherwise, a 2-column matrix, each row of which gives the number of wedges and the number of closed wedges centered at each actor.

See Also

Other triad closure functions: [dynamic_triad_closure\(\)](#), [project_transitivity\(\)](#), [triad_closure\(\)](#), [triad_closure_from_census\(\)](#)

triad	<i>Affiliation network triads</i>
-------	-----------------------------------

Description

These functions create and operate on triads in affiliation networks. In this context, a *triad* is the [schedule](#) of a subset of three distinct actors.

Usage

```
make_triad(
  lambda,
  w,
  actor_names = c("p", "q", "r"),
  event_names = if (sum(c(lambda, w)) == 0) c() else as.character(1:sum(c(lambda, w)))
)

is_triad(graph)

triad_class(
  graph,
  actors = V(graph)[V(graph)$type == FALSE],
  as.partition = TRUE,
  format = "list"
)

layout_triad(
```

```
    triad = NULL,
    lambda = NULL,
    w = NULL,
    scale = 0.3,
    angdir = -1,
    rot = -pi/2,
    rot_lambda = c(0, 0, 0),
    rot_w = pi/12
  )

plot_triad(
  triad = NULL,
  lambda = NULL,
  w = NULL,
  layout = NULL,
  prettify = TRUE,
  cex = 1,
  scale = 0.3,
  angdir = -1,
  rot = -pi/2,
  rot_lambda = c(0, 0, 0),
  rot_w = pi/12,
  actor_names = c("p", "q", "r"),
  event_names = if (sum(c(lambda, w)) == 0) c() else as.character(1:sum(c(lambda, w))),
  xlim = NULL,
  ylim = NULL,
  ...
)

an_triad(...)

is.triad(graph)

triad.class(
  graph,
  actors = V(graph)[V(graph)$type == FALSE],
  as.partition = TRUE,
  format = "list"
)

an.triad(...)

layout.triad(
  triad = NULL,
  lambda = NULL,
  w = NULL,
  scale = 0.3,
  angdir = -1,
```

```

    rot = -pi/2,
    rot_lambda = c(0, 0, 0),
    rot_w = pi/12
  )

plotTriad(
  triad = NULL,
  lambda = NULL,
  w = NULL,
  layout = NULL,
  prettify = TRUE,
  cex = 1,
  scale = 0.3,
  angdir = -1,
  rot = -pi/2,
  rot_lambda = c(0, 0, 0),
  rot_w = pi/12,
  actor_names = c("p", "q", "r"),
  event_names = if (sum(c(lambda, w)) == 0) c() else as.character(1:sum(c(lambda, w))),
  xlim = NULL,
  ylim = NULL,
  ...
)

```

Arguments

lambda	A non-negative integer vector of length three indicating the number of events attended by each pair of actors and not by the third (<i>exclusive</i> events).
w	A non-negative integer indicating the number of events attended by all three actors (<i>inclusive</i> events).
actor_names, event_names	Actor and event names (actor names default to "p", "q", and "r"; event names default to positive integers).
graph	An affiliation network, in some cases must be a triad.
actors	A vector of three actor nodes in graph.
as.partition	Whether to sort the exclusive events, versus reporting them in order of the nodes; defaults to TRUE.
format	Character matched to "list" or "vector"; whether to return the triad class as a list of $\lambda = (x, y, z)$ and w or as a vector of $w, x = \lambda_1, y = \lambda_2$, and $z = \lambda_3$.
triad	An affiliation network with exactly three distinct actors.
scale	A scaling parameter for the entire plot.
angdir	A rotation direction parameter (-1 for clockwise, 1 for counter-clockwise).
rot, rot_lambda, rot_w	Angular orientation parameters for the entire triad, for the exclusive events of two actors, and for the inclusive events of all three actors.
layout	A two-column numeric matrix interpretable as a layout .

prettify	Logical; whether to use <code>prettify_an</code> to adjust the aesthetics of a triad before plotting it.
cex	Node size scaling parameter.
xlim, ylim	Custom bounds on the horizontal and vertical axes.
...	Additional arguments passed to plot.igraph .

Value

An igraph object, a logical value, a matrix of plotting coordinates, or a list of summary parameters `lambda` and `w`.

Examples

```
tr <- make_triad(lambda = c(3,1,1), w = 2)
is_triad(tr)
triad_class(tr)
layout_triad(tr)
plot_triad(tr)
```

| triad_census | *Triad census for affiliation networks* |

Description

Given an affiliation network, tally all actor triads by isomorphism or other congruence class.

Usage

```
triad_census(graph, ..., add.names = TRUE)
```

```
triad_census_an(
  graph,
  scheme = "full",
  method = "batagelj_mrvar",
  ...,
  add.names = TRUE
)
```

```
triad.census.an(...)
```

```
triad_census_full(graph, method = "batagelj_mrvar", ..., add.names = TRUE)
```

```
triad_census_full_batagelj_mrvar(graph, use.integer = FALSE)
```

```
triad_census_full_projection(graph, verbose = FALSE)
```

```

triad_census_difference(
  graph,
  method = "batagelj_mrvar",
  ...,
  add.names = TRUE
)

triad_census_difference_batagelj_mrvar(graph, use.integer = FALSE)

triad_census_difference_projection(graph)

unif_triad_census(graph)

unif.triad.census(graph)

triad_census_binary(graph, method = "batagelj_mrvar", ..., add.names = TRUE)

triad_census_binary_batagelj_mrvar(graph, use.integer = FALSE)

triad_census_binary_projection(graph, verbose = FALSE)

str_triad_census(graph)

structural.triad.census(graph)

simple_triad_census(graph, add.names = TRUE)

simple.triad.census(graph, add.names = TRUE)

```

Arguments

graph	An igraph object, usually an affiliation network.
...	Additional arguments (currently <code>use.integer</code> and <code>verbose</code>) passed to the method function.
add.names	Logical; whether to label the rows and columns of the output matrix.
scheme	Character; the type of triad census to calculate, matched to "full", "difference" (also "uniformity"), "binary" (also "structural"), or "simple".
method	Character; the triad census method to use. Currently only "batagelj_mrvar" is implemented. "projection" calls an inefficient but reliable implementation in R from the first package version that invokes the <code>simple_triad_census()</code> of the <code>actor_projection()</code> of graph.
use.integer	Logical; whether to use the <code>IntegerMatrix</code> class in Rcpp rather than the default <code>NumericMatrix</code> .
verbose	Logical; whether to display progress bars.

Details

The `triad_census_*`(`g`) functions implement the several triad censuses described below. Each census is based on a congruence relation among the triads in an affiliation network, and each function returns a matrix (or, in the "simple" case, a vector) recording the number of triads in each congruence class.

The function `triad_census(g)` masks `triad_census(g)` but calls it in case `g` is not an affiliation network.

Value

An integer matrix of counts of triad congruence classes, with row indices reflecting pairwise exclusive events and column indices reflecting triadwise events.

Triad censuses

Three triad censuses are implemented for affiliation networks:

- The *full triad census* (Brunson, 2015) records the number of triads of each isomorphism class. The classes are indexed by a partition, $\lambda = (\lambda_1 \leq \lambda_2 \leq \lambda_3)$, indicating the number of events attended by both actors in each pair but not the third, and a positive integer, w , indicating the number of events attended by all three actors. The isomorphism classes are organized into a matrix with rows indexed by λ and columns indexed by w , with the partitions λ ordered according to the *revolving door ordering* (Kreher & Stinson, 1999). The main function `triad_census_an` (called from `triad_census` when the `g` argument is an `affiliation_network`) defaults to this census.
- For the analysis of sparse affiliation networks, the full triad census may be less useful than information on whether the extent of connectivity through co-attended events differs between each pair of actors. In order to summarize this information, a coarser triad census can be conducted on classes of triads based on the following congruence relation: Using the indices $\lambda = (x \geq y \geq z)$ and w above, note that the numbers of shared events for each pair and for the triad are $x+w \geq y+w \geq z+w \geq w \geq 0$. Consider two triads congruent if the same subset of these weak inequalities are strictly satisfied. The resulting *difference triad census*, previously called the *uniformity triad census*, implemented as `triad_census_difference`, is organized into a 8×2 matrix with the strictness of the first three inequalities determining the row and that of the last inequality determining the column.
- A still coarser congruence relation can be used to tally how many are connected by at least one event in each distinct way. This relation considers two triads congruent if each corresponding pair of actors both attended or did not attend at least one event not attended by the third, and if the corresponding triads both attended or did not attend at least one event together. The *binary triad census* (Brunson, 2015; therein called the *structural triad census*), implemented as `triad_census_binary`, records the number of triads in each congruence class.
- The *simple triad census* is the 4-entry triad census on a traditional (non-affiliation) network indicating the number of triads of each isomorphism class, namely whether the triad contains zero, one, two, or three links. The function `simple_triad_census` computes the classical (undirected) triad census for an undirected traditional network, or for the actor projection of an affiliation network (if provided), using `triad_census`; if the result doesn't make sense (i.e., the sum of the entries is not the number of triples of nodes), then it instead uses its own, much slower method.

Each of these censuses can be projected from the previous using the function `project_census`. A fourth census, called the *uniformity triad census* and implemented as `unif_triad_census`, is deprecated. Three-actor triad affiliation networks can be constructed and plotted using the `triad` functions. The default method for the two affiliation network-specific triad censuses is adapted from the algorithm of Batagelj and Mrvar (2001) for calculating the classical triad census for a directed graph.

References

- Kreher, D.L., & Stinson, D.R. (1999). Combinatorial algorithms: generation, enumeration, and search. *SIGACT News*, 30(1), 33–35.
- Batagelj, V., & Mrvar, A. (2001). A subquadratic triad census algorithm for large sparse networks with small maximum degree. *Social Networks*, 23(3), 237–243.
- Brunson, J.C. (2015). Triadic analysis of affiliation networks. *Network Science*, 3(4), 480–508.

See Also

Original **igraph** functions: `triad_census()`

Other triad census functions: `project_census()`, `triad_closure_from_census()`, `triad_tallies`

Examples

```
data(women_clique)
(tc <- triad_census(women_clique, add.names = TRUE))
sum(tc) == choose(vcount(actor_projection(women_clique)), 3)
```

triad_closure	<i>Triad closure for affiliation networks</i>
---------------	---

Description

Given an affiliation network and a vector of actor node IDs, calculate a specified measure of triad closure centered at the nodes.

Usage

```
triad_closure(graph, ...)

triad_closure_an(graph, method = "wedges", ...)

triad_closure_via_triads(
  graph,
  actors = V(graph)[V(graph)$type == FALSE],
  type = "global",
  ...
)

triad_closure_from_centered_triads(
```

```
    triad_list,  
    type = "global",  
    ...,  
    measure = NULL,  
    triads.fun = NULL  
  )  
  
  triad_closure_via_wedges(  
    graph,  
    actors = V(graph)[V(graph)$type == FALSE],  
    type = "global",  
    ...,  
    measure = NULL,  
    wedges.fun = NULL  
  )  
  
  triad_closure_watts_strogatz(  
    graph,  
    actors = V(graph)[V(graph)$type == FALSE],  
    type = "global"  
  )  
  
  triad_closure_classical(  
    graph,  
    actors = V(graph)[V(graph)$type == FALSE],  
    type = "global"  
  )  
  
  triad_closure_opsahl(  
    graph,  
    actors = V(graph)[V(graph)$type == FALSE],  
    type = "global"  
  )  
  
  triad_closure_twomode(  
    graph,  
    actors = V(graph)[V(graph)$type == FALSE],  
    type = "global"  
  )  
  
  triad_closure_liebig_rao_0(  
    graph,  
    actors = V(graph)[V(graph)$type == FALSE],  
    type = "global"  
  )  
  
  triad_closure_unconnected(  
    graph,
```

```

    actors = V(graph)[V(graph)$type == FALSE],
    type = "global"
)

triad_closure_liebig_rao_3(
  graph,
  actors = V(graph)[V(graph)$type == FALSE],
  type = "global"
)

triad_closure_completely_connected(
  graph,
  actors = V(graph)[V(graph)$type == FALSE],
  type = "global"
)

triad_closure_exclusive(
  graph,
  actors = V(graph)[V(graph)$type == FALSE],
  type = "global"
)

triad_closure_projection(
  graph,
  actors = V(graph)[V(graph)$type == FALSE],
  type = "global"
)

```

Arguments

graph	An affiliation network.
...	Measure specifications passed to wedges .
method	Character; for a given measure, whether to use the measure-specific wedge census ("wedges") or the measure-specific calculation on the centered triad census ("triads").
actors	A vector of actor nodes in graph.
type	The type of statistic, matched to "global", "local", or "raw".
triad_list	A list of triad isomorphism classes in matrix format, as produced by centered_triads .
measure	Character; the measure of triad closure, used as the suffix * to triad_closure_*. Matched to "classical" (also "watts_strogatz"), "twomode" (also "opsahl"), "unconnected" (also "liebig_rao_0"), "completely_connected" (also "liebig_rao_3"), or "exclusive".
triads.fun	A custom triad closure calculation. It must accept a vector of <i>centered</i> triad isomorphism classes, encoded as vectors w, x, y, and z, and return a 2-row integer matrix recording the number of wedges of the desired measure centered at the second actor, and involving the other two actors, of each triad.

wedges.fun A custom wedge census function. It must accept an affiliation network graph and a single actor node ID actor and may have any additional parameters. It must return a named list with values wedges a numeric matrix of node IDs whose columns record the wedges centered at actor and closed a logical vector recording whether each wedge is closed. Overrides measure.

Details

The triad_closure_* functions implement the several measures of triad closure described below. Each function returns a single global statistic, a vector of local statistics, or a matrix of local denominators and numerators from which the global and local statistics can be recovered.

The function triad_closure_projection recapitulates triad_closure_watts_strogatz() by invoking the bipartite_projection() and transitivity() functions in igraph.

Value

If type is "global", the global statistic for graph (a single numeric value); if "local", the local statistics for actors (a numeric vector); if "raw", a 2-column matrix, each row of which gives the number of wedges and of closed wedges centered at actors.

Measures of triad closure

Each measure of triad closure is defined as the proportion of wedges that are closed, where a *wedge* is the image of a specified two-event triad W under a specified subcategory of graph maps C subject to a specified congruence relation \sim , and where a wedge is *closed* if it is the image of such a map that factors through a canonical inclusion of W to a specified self-dual three-event triad X .

The alcove, wedge, maps, and congruence can be specified by numerical codes as follows (no plans exist to implement more measures than these):

- alcove:
 - 0: $T_{(1,1,1),0}$
 - 1: $T_{(1,1,0),1}$ **(not yet implemented)**
 - 2: $T_{(1,0,0),2}$ **(not yet implemented)**
 - 3: $T_{(0,0,0),3}$ **(not yet implemented)**
- wedge:
 - 0: $T_{(1,1,0),0}$
 - 1: $T_{(1,0,0),1}$ **(not yet implemented)**
 - 2: $T_{(0,0,0),2}$ **(not yet implemented)**
- maps:
 - 0: all graph maps (injective on actors)
 - 1: injective graph maps
 - 2: induced injective graph maps
- congruence:
 - 0: same actor and event images (equivalence)
 - 1: same actor images, structurally equivalent event images

- 2: same actor images

Some specifications correspond to statistics of especial interest:

- $0, 0, 0, 2$: the classical clustering coefficient (Watts & Strogatz, 1998), evaluated on the unipartite actor projection
- $0, 0, 1, 0$: the two-mode clustering coefficient (Opsahl, 2013)
- $0, 0, 2, 0$: the unconnected clustering coefficient (Liebig & Rao, 2014)
- $3, 2, 2, 0$: the completely connected clustering coefficient (Liebig & Rao, 2014) (**not yet implemented**)
- $0, 0, 2, 1$: the exclusive clustering coefficient (Brunson, 2015)
- $0, 0, 2, 2$: the exclusive clustering coefficient

See Brunson (2015) for a general definition and the aforementioned references for discussions of each statistic.

References

Watts, D.J., & Strogatz, S.H. (1998). Collective dynamics of "small-world" networks. *Nature*, 393(6684), 440–442.

Opsahl, T. (2013). Triadic closure in two-mode networks: Redefining the global and local clustering coefficients. *Social Networks*, 35(2), 159–167. Special Issue on Advances in Two-mode Social Networks.

Liebig, J., & Rao, A. (2014). Identifying influential nodes in bipartite networks using the clustering coefficient. Pages 323–330 of: *Proceedings of the tenth international conference on signal-image technology and internet-based systems*.

Brunson, J.C. (2015). Triadic analysis of affiliation networks. *Network Science*, 3(4), 480–508.

See Also

Original **igraph** functions: [transitivity\(\)](#)

Other triad closure functions: [dynamic_triad_closure\(\)](#), [project_transitivity\(\)](#), [transitivity_an\(\)](#), [triad_closure_from_census\(\)](#)

Examples

```
data(women_clique)
maply(
  triad_closure,
  measure = c("classical", "twomode", "unconnected", "exclusive"),
  MoreArgs = list(graph = women_clique, type = "local")
)
data(women_group)
cbind(
  triad_closure_watts_strogatz(women_group, type = "local"),
  triad_closure_opsahl(women_group, type = "local"),
  triad_closure_liebig_rao_0(women_group, type = "local"),
  triad_closure_exclusive(women_group, type = "local")
)
```

`triad_closure_from_census`*Global triad closure from a triad census*

Description

Given a triad census of a suitable scheme, calculate a global measure of triad closure for the associated affiliation network.

Usage

```
triad_closure_from_census(  
  census,  
  scheme = NULL,  
  alcove = 0,  
  wedge = 0,  
  maps = 0,  
  congruence = 0,  
  measure = NULL,  
  open.fun = NULL,  
  closed.fun = NULL,  
  counts = FALSE  
)
```

```
triad_closure_from_simple_census(  
  census,  
  alcove = 0,  
  wedge = 0,  
  maps = 0,  
  congruence = 0,  
  open.fun = NULL,  
  closed.fun = NULL,  
  counts = FALSE  
)
```

```
triad_closure_from_binary_census(  
  census,  
  alcove = 0,  
  wedge = 0,  
  maps = 0,  
  congruence = 0,  
  open.fun = NULL,  
  closed.fun = NULL,  
  counts = FALSE  
)
```

```
triad_closure_from_difference_census(  
  census,  
  alcove = 0,  
  wedge = 0,  
  maps = 0,  
  congruence = 0,  
  open.fun = NULL,  
  closed.fun = NULL,  
  counts = FALSE  
)
```

```
census,  
alcove = 0,  
wedge = 0,  
maps = 0,  
congruence = 0,  
open.fun = NULL,  
closed.fun = NULL,  
counts = FALSE  
)  
  
triad_closure_from_full_census(  
  census,  
  alcove = 0,  
  wedge = 0,  
  maps = 0,  
  congruence = 0,  
  open.fun = NULL,  
  closed.fun = NULL,  
  counts = FALSE  
)  
  
wedges_from_full_census(census, open.fun, closed.fun)  
  
wedges_from_census(...)  
  
wedgcount_census(...)  
  
wedgcount.census(...)  
  
triad_closure_from_census_original(  
  census,  
  scheme = NULL,  
  alcove = 0,  
  wedge = 0,  
  maps = 0,  
  congruence = 0,  
  measure,  
  open.fun,  
  closed.fun,  
  counts = FALSE  
)  
  
transitivity_from_census(...)  
  
transitivity.census(...)
```

Arguments

census	Numeric matrix or vector; an affiliation network triad census. It is treated as binary or simple if its dimensions are 4-by-2 or 4-by-1, respectively, unless otherwise specified by scheme; otherwise it is treated as full.
scheme	Character; the type of triad census provided, matched to "full", "difference" (also "uniformity"), "binary" (also "structural"), or "simple".
alcove, wedge, maps, congruence	Choice of alcove, wedge, maps, and congruence (see Details).
measure	Character; the measure of triad closure (matched to "classical", "watts_strogatz", "twomode", "opsahl", "unconnected", "liebig_rao_0", "completely_connected", "liebig_rao_3", "exclusive", "allact", "indequ", "indstr", "inact", "injequ", or "injstr"). Overrides alcove, wedge, maps, and congruence.
open.fun, closed.fun	Functions to calculate the open and closed wedge count for a triad (when scheme is "full") or a triad census (otherwise), in order to calculate a custom measure of triad closure. Override measure.
counts	Logical; whether to return open and closed wedge counts instead of the quotient.
...	Arguments passed from deprecated functions to their replacements.

Details

Each global measure of triad closure can be recovered from the full triad census, and some can be recovered from smaller censuses. This function verifies that a given census is sufficient to recover a given measure of triad closure and, if it is, returns its value.

Value

Output equivalent to that of `triad_closure()`.

Triad censuses

Three triad censuses are implemented for affiliation networks:

- The *full triad census* (Brunson, 2015) records the number of triads of each isomorphism class. The classes are indexed by a partition, $\lambda = (\lambda_1 \leq \lambda_2 \leq \lambda_3)$, indicating the number of events attended by both actors in each pair but not the third, and a positive integer, w , indicating the number of events attended by all three actors. The isomorphism classes are organized into a matrix with rows indexed by λ and columns indexed by w , with the partitions λ ordered according to the *revolving door ordering* (Kreher & Stinson, 1999). The main function `triad_census_an` (called from `triad_census` when the graph argument is an `affiliation_network`) defaults to this census.
- For the analysis of sparse affiliation networks, the full triad census may be less useful than information on whether the extent of connectivity through co-attended events differs between each pair of actors. In order to summarize this information, a coarser triad census can be conducted on classes of triads based on the following congruence relation: Using the indices $\lambda = (x \geq y \geq z)$ and w above, note that the numbers of shared events for each pair and for the triad are $x+w \geq y+w \geq z+w \geq w \geq 0$. Consider two triads congruent if the same subset of

these weak inequalities are strictly satisfied. The resulting *difference triad census*, previously called the *uniformity triad census*, implemented as `triad_census_difference`, is organized into a 8×2 matrix with the strictness of the first three inequalities determining the row and that of the last inequality determining the column.

- A still coarser congruence relation can be used to tally how many are connected by at least one event in each distinct way. This relation considers two triads congruent if each corresponding pair of actors both attended or did not attend at least one event not attended by the third, and if the corresponding triads both attended or did not attend at least one event together. The *binary triad census* (Brunson, 2015; therein called the *structural triad census*), implemented as `triad_census_binary`, records the number of triads in each congruence class.
- The *simple triad census* is the 4-entry triad census on a traditional (non-affiliation) network indicating the number of triads of each isomorphism class, namely whether the triad contains zero, one, two, or three links. The function `simple_triad_census` computes the classical (undirected) triad census for an undirected traditional network, or for the actor projection of an affiliation network (if provided), using `triad_census`; if the result doesn't make sense (i.e., the sum of the entries is not the number of triples of nodes), then it instead uses its own, much slower method.

Each of these censuses can be projected from the previous using the function `project_census`. A fourth census, called the *uniformity triad census* and implemented as `unif_triad_census`, is deprecated. Three-actor triad affiliation networks can be constructed and plotted using the `triad` functions.

The default method for the two affiliation network-specific triad censuses is adapted from the algorithm of Batagelj and Mrvar (2001) for calculating the classical triad census for a directed graph.

Measures of triad closure

Each measure of triad closure is defined as the proportion of wedges that are closed, where a *wedge* is the image of a specified two-event triad W under a specified subcategory of graph maps C subject to a specified congruence relation \sim , and where a wedge is *closed* if it is the image of such a map that factors through a canonical inclusion of W to a specified self-dual three-event triad X .

The alcove, wedge, maps, and congruence can be specified by numerical codes as follows (no plans exist to implement more measures than these):

- alcove:
 - 0: $T_{(1,1,1),0}$
 - 1: $T_{(1,1,0),1}$ (**not yet implemented**)
 - 2: $T_{(1,0,0),2}$ (**not yet implemented**)
 - 3: $T_{(0,0,0),3}$ (**not yet implemented**)
- wedge:
 - 0: $T_{(1,1,0),0}$
 - 1: $T_{(1,0,0),1}$ (**not yet implemented**)
 - 2: $T_{(0,0,0),2}$ (**not yet implemented**)
- maps:
 - 0: all graph maps (injective on actors)
 - 1: injective graph maps
 - 2: induced injective graph maps

- congruence:
 - 0: same actor and event images (equivalence)
 - 1: same actor images, structurally equivalent event images
 - 2: same actor images

Some specifications correspond to statistics of especial interest:

- 0, 0, 0, 2: the classical clustering coefficient (Watts & Strogatz, 1998), evaluated on the uni-partite actor projection
- 0, 0, 1, 0: the two-mode clustering coefficient (Opsahl, 2013)
- 0, 0, 2, 0: the unconnected clustering coefficient (Liebig & Rao, 2014)
- 3, 2, 2, 0: the completely connected clustering coefficient (Liebig & Rao, 2014) (**not yet implemented**)
- 0, 0, 2, 1: the exclusive clustering coefficient (Brunson, 2015)
- 0, 0, 2, 2: the exclusive clustering coefficient

See Brunson (2015) for a general definition and the aforementioned references for discussions of each statistic.

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- Kreher, D.L., & Stinson, D.R. (1999). Combinatorial algorithms: generation, enumeration, and search. *SIGACT News*, 30(1), 33–35.
- Batagelj, V., & Mrvar, A. (2001). A subquadratic triad census algorithm for large sparse networks with small maximum degree. *Social Networks*, 23(3), 237–243.
- Brunson, J.C. (2015). Triadic analysis of affiliation networks. *Network Science*, 3(4), 480–508.
- Watts, D.J., & Strogatz, S.H. (1998). Collective dynamics of "small-world" networks. *Nature*, 393(6684), 440–442.
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- Liebig, J., & Rao, A. (2014). Identifying influential nodes in bipartite networks using the clustering coefficient. Pages 323–330 of: *Proceedings of the tenth international conference on signal-image technology and internet-based systems*.
- Brunson, J.C. (2015). Triadic analysis of affiliation networks. *Network Science*, 3(4), 480–508.

See Also

Other triad census functions: [project_census\(\)](#), [triad_census\(\)](#), [triad_tallies](#)

Other triad closure functions: [dynamic_triad_closure\(\)](#), [project_transitivity\(\)](#), [transitivity_an\(\)](#), [triad_closure\(\)](#)

whigs

Membership network of American Whigs.

Description

These data record the membership of 136 colonial Americans in 5 Whig organizations.

Format

An affiliation network; see [is_an](#).

Source

Fischer, D.H. (1994). *Paul Revere's Ride*. Oxford University Press. https://books.google.com/books?id=knC-kTFI9_gC <https://github.com/kjhealy/revere>

women_clique

Clique of women connected by event coattendance in Old City.

Description

These data record the participation of 5 African-American women in 5 social activities.

Format

An affiliation network; see [is_an](#).

Source

Davis, A., Gardner, B.B., & Gardner, M.R. (1941). *Deep South: A Social Anthropological Study of Caste and Class*. Columbia, SC: University of South Carolina Press. <http://books.google.com/books?id=HGIdAAAAIAAJ>

women_group

Group of women connected by event coattendance in Old City.

Description

These data record the attendance of 18 white women at 14 social events over a 9-month period.

Format

An affiliation network; see [is_an](#). Events carry a time attribute equal to the number of days since the previous 31 December.

Source

Davis, A., Gardner, B.B., & Gardner, M.R. (1941). *Deep South: A Social Anthropological Study of Caste and Class*. Columbia, SC: University of South Carolina Press. <http://books.google.com/books?id=HGIdAAAAIAAJ>

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